

- (1) **Warm-up/Motivation:** Consider 5 teams. Can you create a tournament where each team plays against *exactly* 2 other teams?

- (2) Can you create a tournament where each of the 5 teams plays against exactly 3 other teams?

- (3) **Question:** When is it possible for  $n$  teams to play exactly  $r$  different teams?

**Definitions:**

- A **Graph**  $G$  is made of two sets: the \_\_\_\_\_,  $V = \{v_1, v_2, \dots, v_n\}$ , and a set of pairs of vertices  $v_i v_j$  called the \_\_\_\_\_,  $E$ .
- Instead of writing graphs as sets, we most often **draw them as diagrams**. We draw vertices as dots, labeled with the vertex name, and edges as lines between two vertices.

**Vocab:**

- The **degree** of a vertex is the number of edges it touches.

(4) **Examples:** Make a table!

Graph

number of edges

list of degrees

sum of degrees

(5) What patterns/observations can you make?

(6) **The First Theorem of Graph Theory:**

(7) What can we conclude about our original question?